

**Practice with Power Functions**

1. For a certain light bulb, the intensity of the light, measured in lux, can be represented by the function  $I(d) = 100d^{-2}$ , where  $d$  is the distance measured in feet from the light bulb.
  - a. What is the intensity of the light bulb if you are 5 feet away from the light bulb?
  - b. What is the intensity of the light bulb if you are 10 feet away from the light bulb?
  
2. The distance that a planet is from the sun can be approximated by the power function  $f(x) = 92.9x^{\frac{2}{3}}$ , where  $x$  is the number of years for a planet to orbit the sun, and  $f(x)$  is the distance (in millions of miles) the planet is from the sun.
  - a. Uranus takes about 84 years to orbit the sun. What is its distance from the sun?
  - b. Mars takes 1.88 years to orbit the sun. What is its distance from the sun?
  
3. The power (in watts) produced by a windmill is related to the speed of the wind by the formula  $P(v) = .015v^3$ , where  $v$  is the wind speed in miles per hour, and  $P(v)$  is the power (in watts).
  - a. If the wind is blowing at 10 mph, how much power is generated?
  - b. If the wind is blowing at 20 mph, how much power is generated?

**Rational Exponents**

Rewrite each expression using rational exponent notation.

1. $\sqrt[3]{15}$	2. $\sqrt[4]{19}$	3. $(\sqrt[2]{5})^3$
4. $(\sqrt[8]{11})^5$	5. $\sqrt[3]{5^2}$	6. $\sqrt[8]{21^7}$

Rewrite the expression using radical notation.

7. $7^{\frac{1}{4}}$	8. $13^{\frac{1}{3}}$	9. $5^{\frac{3}{4}}$
10. $8^{\frac{4}{5}}$	11. $9^{\frac{5}{3}}$	12. $17^{\frac{5}{2}}$

Find the indicated real  $n^{\text{th}}$  roots of  $a$ .

13.  $n = 2, a = 49$

14.  $n = 3, a = -8$

Evaluate the expression using a calculator. Round the result to three decimal places when appropriate.

15. $\sqrt[5]{-32768}$	16. $\sqrt[8]{1354}$	17. $5^{\frac{1}{7}}$
18. $15^{-\frac{1}{5}}$	19. $(\sqrt[3]{152})^2$	20. $(-170)^{-\frac{2}{5}}$

Solve the equation. Round your answer to three decimal places when appropriate.

21. $x^6 = 729$	22. $5x^3 = -1080$	23. $(x-3)^4 = 16$
24. $-x^5 = 60$	25. $x^3 - 13 = 25$	26. $x^8 + 10 = 70$

Simplify the expression. Assume all variables are positive.

1. $5^{\frac{1}{4}} \cdot 5^{\frac{3}{4}}$	2. $\left(7^{\frac{1}{3}}\right)^6$	3. $\sqrt[4]{2} \cdot \sqrt[4]{8}$
4. $\left(5^{\frac{1}{2}}\right)^4$	5. $\sqrt[3]{\frac{8}{27}}$	6. $x^{\frac{2}{3}} \cdot x^{\frac{7}{3}}$
7. $\left(y^{\frac{1}{4}}\right)^8$	8. $\sqrt{9x^4}$	9. $\sqrt[5]{\frac{x^{15}}{y^5}}$
10. $2^{\frac{1}{2}} \cdot 2^{\frac{5}{2}}$	11. $\left(6^{\frac{1}{3}}\right)^6$	12. $\frac{1}{8^{\frac{1}{3}}}$
13. $\frac{18^{\frac{1}{2}}}{2^{\frac{1}{2}}}$	14. $\left(2^{\frac{1}{2}} \cdot 2^{\frac{1}{3}}\right)^6$	15. $\left(\frac{7^3}{8^3}\right)^{\frac{1}{3}}$
16. $\frac{6^{\frac{3}{2}} \cdot 8^{\frac{3}{2}}}{12^{\frac{3}{2}}}$	17. $\frac{15^{\frac{3}{7}}}{15^{\frac{2}{7}}}$	18. $\left(6^{\frac{3}{5}} \cdot 2^{\frac{3}{5}}\right)^{-5}$
19. $\sqrt[5]{8} \cdot \sqrt[5]{4}$	20. $\sqrt[3]{10} \cdot \sqrt[3]{100}$	21. $\left(\sqrt[3]{2} \cdot \sqrt{2}\right)^{12}$
22. $\frac{\sqrt[3]{250}}{\sqrt[3]{2}}$	23. $\frac{\sqrt[5]{8} \cdot \sqrt[5]{8}}{\sqrt[5]{2}}$	24. $\frac{\sqrt[3]{10}}{\sqrt[4]{10}}$

25. $x^{\frac{1}{2}} \cdot x^{\frac{1}{3}}$	26. $(z^{12})^{\frac{1}{2}}$	27. $\sqrt[4]{\frac{y^{12}}{x^8}}$
28. $\frac{x^{\frac{4}{3}}y}{xy^{\frac{2}{3}}}$	29. $\frac{x^{\frac{4}{3}}yz^{\frac{2}{5}}}{x^{\frac{1}{3}}z^{\frac{3}{5}}}$	30. $\frac{\sqrt[3]{x^6}}{\sqrt[3]{8x} \cdot \sqrt[3]{x^{11}}}$
<p>31. The formula <math>t = 2\pi\sqrt{\frac{L}{9.8}}</math> is used to estimate the number of seconds <math>t</math> it takes a pendulum of length <math>L</math> meters to make one complete swing.</p> <p>a. How many seconds does it take a pendulum of <math>L = 1.5</math> meters to make one complete swing?</p> <p>b. How many seconds does it take a pendulum of length 2.5 meters to make one complete swing?</p> <p>c. The length of a pendulum is doubled. How many times longer does it take the pendulum to make one complete swing?</p>		

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32. $(x^{\sqrt{3}})^{\sqrt{3}}$	33. $\left(\frac{x^\pi}{y^{2\pi}}\right)^{\frac{1}{\pi}}$	34. $(x^{\sqrt{2}}y^{\sqrt{8}})^{\sqrt{2}}$

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Graph the function. Then state the domain and range.

1.  $f(x) = \frac{1}{2}\sqrt[3]{x}$

2.  $f(x) = \sqrt[3]{x} + 2$

3.  $f(x) = \sqrt[3]{x-2}$

4.  $f(x) = \frac{1}{4}x^{\frac{1}{3}} + 3$

5.  $f(x) = 2\sqrt[3]{x-1} + 3$

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1.  $x^{\frac{3}{2}} = 8$

2.  $x^{\frac{2}{3}} - 4 = 5$

3.  $5x^{\frac{3}{4}} = 135$

4.  $(3x - 2)^{\frac{1}{2}} = 4$  (6)